

# Development of a Deep Recurrent Neural Network Controller for Flight Applications

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# Outline

- Inspiration
- DLC Limitations and Research Goals
- Background – Direct Policy Search
- Flight Vehicle (Plant) Model
- Architecture - Deep Learning Flight Control
- Optimization - Deep Learning Controller
- Simulation Results
- Conclusions
- Future Work

# Inspiration

## Deep Learning (DL):

- Dominant performance in multiple machine learning areas:  
Speech, language, vision, face recognition, etc.
- Replaces time consuming typical hand-tuned machine learning methods

## Key Breakthroughs in establishing Deep Learning:

- Optimization methods: Stochastic Gradient Descent, Hessian-free, Nestorov's momentum, etc.
- Deep recurrent neural network (RNN) architectures: deep stacked RNN, deep bidirectional RNN, etc.
- RNN Modules: Gated Recurrent Unit (GRU) and Long Short Term Memory (LSTM)
- Automatic gradient computation
- Parallel computing

## Connecting Deep Learning to Control:

- Guided Policy Search – uses trajectory optimization to assist policy learning (S. Levine and V. Koltun, 2013)
- Hessian-free Optimization– deep RNN learning control with uncertainties (I. Sutskever, 2013)



# DLC Limitations and Research Goals

## Policy Search/Deep Learning (DL) Control Limitations:

- Large number of computations at each time step
- No standard training procedures for control tasks
- Few analysis tools for deep neural network architectures
- Non-convex form of optimization provides few guarantees
- Lack of research in optimization with regards to robustness
- Most RL approaches use the combination of modeled dynamics and real-life trial to tune policy (not useful for flight control)

### Research Goals

Develop a robust deep recurrent neural network (RNN) controller with gated recurrent unit (GRU) modules for a highly agile high-speed flight vehicle that is trained using a set of sample trajectories that contain disturbances, aerodynamic uncertainties, and significant control attenuation/amplification in the plant dynamics during optimization.

# Direct Policy Search Background

## Reinforcement Learning (RL):

Develop methods to sufficiently train an agent by maximizing a cost function through repeated interactions with its environment.

## Markovian Dynamics

$$x_{t+1} = f(x_t, u_t) + w, \quad x_0 \sim p(x_0)$$

Find Parametrized Policy ( $\pi_{\Theta}^*$ ) for the finite horizon problem:

$$\pi_{\Theta}^* = \operatorname{argmax}_{\pi_{\Theta}} J_{\Theta} = \operatorname{argmax}_{\pi} \sum_{t=1}^{t_f} \gamma^t E[r(x_t, u_t) | \pi_{\Theta}], \quad \gamma \in [0,1]$$

## Certainty-Equivalence (CE) Assumption:

The optimal policy for the learned model corresponds to the optimal policy for the true dynamics

## How to use models for long-term predictions:

1. Stochastic inference (i.e. trajectory sampling)
2. Deterministic approximate inference

\*M. P. Deisenroth, et al., "A survey on policy search for robotics," Foundations and Trends in Robotics, vol. 2, 2013.

# Direct Policy Search Background

## Stochastic Sampling:

Expected long-term reward:

$$J_{\Theta} = \operatorname{argmax}_{\pi} \sum_{t=1}^{t_f} \gamma^t \mathbb{E}[r(x_t, u_t) | \pi_{\Theta}]$$

Approximation of  $J_{\Theta}$ :

$$\tilde{J}_{\Theta} = \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^{t_f} \gamma^t r(x_t^i) \quad \lim_{N \rightarrow \infty} \tilde{J}_{\Theta} = J_{\Theta}$$

## Deterministic Approximations:

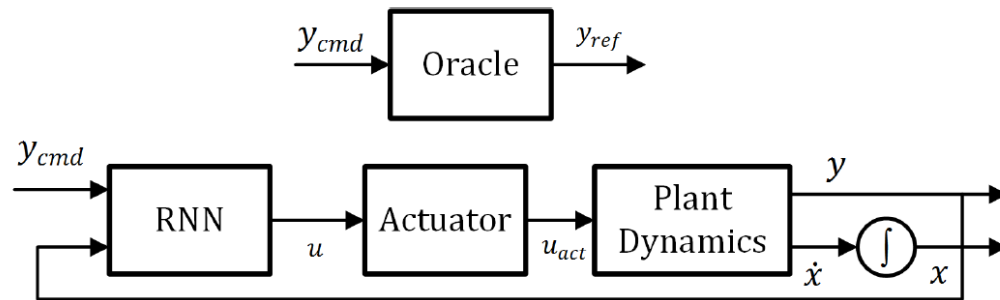
Approximation of  $p(x_t)$ : (e. g. Unscented Transformation or Moment Matching)

$$\mathbb{E}[r(x_t, u_t) | \pi_{\Theta}] = \int r(x_t) p(x_t) dx_t$$

$$p(x_t) \cong \mathcal{N}(x_t | \mu_t^x, \Sigma_t^x)$$

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# Deep Learning based Flight Control



Deep Learning Training Architecture

## Generalized Form of the Discrete Plant Dynamics

$$\begin{aligned}
 x_{t+1} &= f(x_t, (\lambda_u(u_t^{act} + \rho_u)) + d_u, \rho_\alpha, \rho_q) + \zeta_p \\
 y_t &= f(x_t, (\lambda_u(u_t^{act} + \rho_u)) + d_u, \rho_\alpha, \rho_q) + \zeta_p
 \end{aligned}$$

$x_t$  are the states of the plant

$u_t^{act}$  is the actuator output

$y_t$  is the output vector

$\zeta_p$  is the plant noise

$\lambda_u$  is the control effectiveness

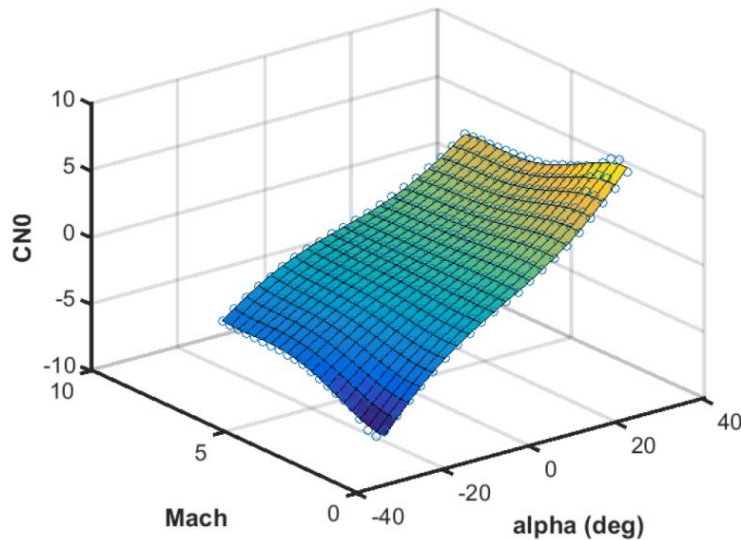
$d_u$  is an input disturbance

$\rho_u, \rho_\alpha, \rho_q$  are uncertainty parameters

# Flight Vehicle Model

## Longitudinal Rigid Body Dynamics:

$$\begin{aligned}\dot{V}_T &= \frac{1}{m}(T\cos(\alpha) - D) - g\sin(\theta - \alpha) \\ \dot{\alpha} &= \frac{1}{mV_T}(-T\sin(\alpha) - L) + q + \frac{g}{V_T}\cos(\theta - \alpha) \\ \dot{\Theta} &= q \\ \dot{q} &= \frac{M}{I_{YY}} \quad x = [V_T, \alpha, \Theta, q, h] \\ \dot{h} &= V_T\sin(\theta - \alpha) \quad y = [\alpha, q, A_z, \bar{q}]\end{aligned}$$



## Force and Moment Equations:

$$\begin{aligned}A &\approx \frac{1}{2}\rho V_T^2 S C_A & L &= N\cos(\alpha) - A\sin(\alpha) \\ N &\approx \frac{1}{2}\rho V_T^2 S C_N & D &= N\sin(\alpha) + A\cos(\alpha) \\ M &\approx \frac{1}{2}\rho V_T^2 S c_{ref} C_m\end{aligned}$$

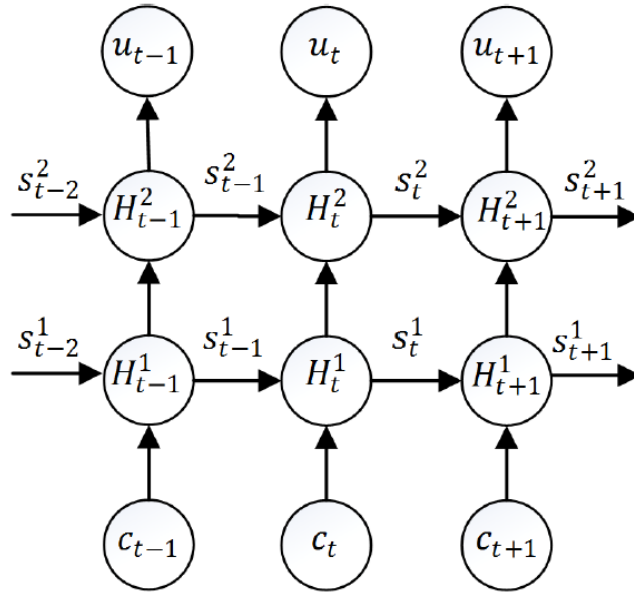
## Aerodynamic Coefficients (Longitudinal):

$$\begin{aligned}C_A &= C_{A_{ALT}}(h, M) + C_{A_{AB}}(\alpha, M) \\ &\quad + \sum_{i=1}^4 C_{A_{\delta_i}}(\alpha, M, \delta_i) \\ C_N &= C_{N_0}(\alpha, M) + \sum_{i=1}^4 C_{N_{\delta_i}}(\alpha, M, \delta_i) \\ C_m &= C_{m_0}(\alpha, M) + \sum_{i=1}^4 C_{m_{\delta_i}}(\alpha, M, \delta_i) \\ &\quad + C_{m_q}(\alpha, M, q) + q\rho_q + \alpha\rho_\alpha\end{aligned}$$



# Deep Learning Controller - Architecture

## Stacked Recurrent Neural Network (S-RNN)



## Controller Input Vector:

$$c_t = [e_i, \alpha, q, \bar{q}]$$

$$e = y_{sel} - y_{cmd}$$

$$e_i = \int_0^{t_f} e \, dt$$

## Algorithm 1 Gated Recurrent Units (GRU)

- 1:  $z = \sigma(c_t U^u + s_{t-1} W^u + b_1)$
- 2:  $r = \sigma(c_t U^r + s_{t-1} W^r + b_2)$
- 3:  $h = \tanh(c_t U^h + (s_{t-1} * r) W^h + b_3)$
- 4:  $s_t = (1 - z) * h + z * s_{t-1}$
- 5:  $*$  represents element-wise multiplication

$$u_t = s_t V + c$$

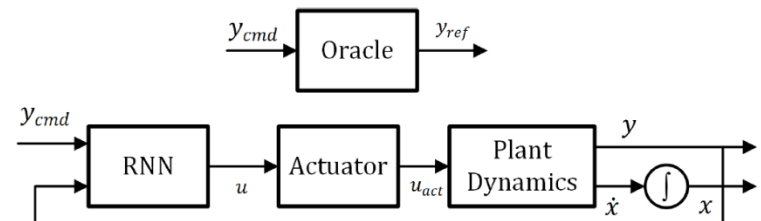
$\Theta_i$  matrix of parameters for each GRU module

$$\Theta_i = [U^u, W^u, U^r, W^r, U^h, W^h, b_1, b_2, b_3]$$

$\Theta$  total parameters of the controller

$$\Theta = [\Theta_1, \Theta_2, \dots, \Theta_L, V, c]$$

$L$  total layers of GRU modules



# Deep Learning Controller - Optimization

Estimated Expected Long-Term Reward:

$$\tilde{J}(\Theta) = \frac{1}{N} \sum_{i=1}^N J_i(\Theta)$$

Cost function for each trajectory, i:

$$J_i(\Theta) = \sum_{t=0}^{t_f} \gamma^t \chi(x_t, u_t)$$

label = P: only uncertainties

label = R: uncertainties, noise, and disturbances

**Instantaneous Measurement:**

$$\chi(x_t, u_t) = \begin{cases} k_1 e_t^2 + k_2 f_u^2 & \text{if label} = P \\ k_3 f_e^2 + k_4 f_u^2 & \text{if label} = R \end{cases}$$

$$f_e = \max(|e_t| - b_e, 0)$$

$$f_u = \max(|\dot{u}_t| - b_{\dot{u}}, 0)$$

**Time-varying funnel:**

$$\beta_{\dot{u}}(t) = \{x \in \mathbb{R}^n | U(x, t) \leq b_{\dot{u}}(t)\}$$

$$\beta_e(t) = \{x \in \mathbb{R}^n | E(x, t) \leq b_e(t)\}$$

TABLE I

RANGE OF INITIAL CONDITIONS AND UNCERTAINTY VARIABLES

|                        | MIN | MAX |             | MIN  | MAX |
|------------------------|-----|-----|-------------|------|-----|
| $\alpha_0[\text{deg}]$ | -25 | 25  | $R_\alpha$  | -0.5 | 0.1 |
| $q_0[\text{deg/sec}]$  | -75 | 75  | $R_q$       | -7   | 5   |
| $Mach_0$               | 1.0 | 2.0 | $R_u$       | -5   | 5   |
| $alt_0[\text{km}]$     | 7   | 14  | $\Lambda_u$ | 0.25 | 3.0 |

$$[R_\alpha, R_q, R_u, \Lambda_u] \sim \text{Uniform}[min, max]$$

$[\rho_\alpha^i, \rho_q^i, \rho_u^i, \lambda_u^i]$  are uncertainties (ith trajectory)

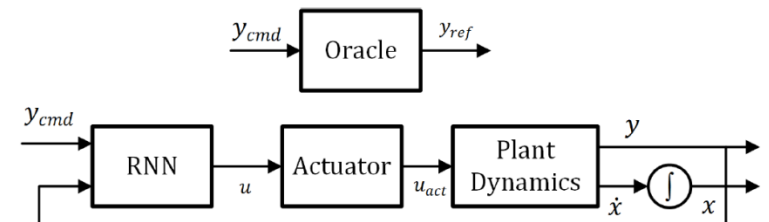
$N$  is the number of sampled trajectories

$t_f$  is the duration of each sampled trajectory

$k_1, k_2, k_3, k_4$  are positive constant gains

$b_e, b_{\dot{u}}$  are static constant bounds of the funnel

$$e_t = y_{sel} - y_{ref}$$



# DLC – Incremental Training

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**Algorithm 2** Incremental Training Procedure

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- 1: Randomly initialize controller parameters ( $\Theta$ )
  - 2: STEP 1: Optimize  $\Theta$  for RNN/GRU using cost function (21) with linear dynamics and labels=P
  - 3: STEP 2: Re-optimize  $\Theta$  using nonlinear dynamics, labels=P, with small uncertainties in aerodynamics
  - 4: STEP 3: Re-optimize  $\Theta$  using nonlinear dynamics, labels=(R,P), with uncertainties, disturbances, and noise
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## Optimization Specifications:

RNN/GRU, RNN, TD-FNN

L-BFGS (Quasi-Newton) Optimization

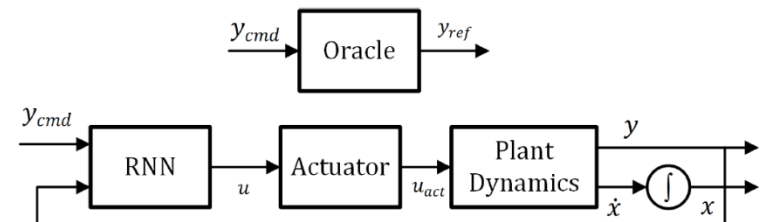
N = 2,970 Sample Trajectories

540 Performance Trajectories

2,430 Robust Trajectories

3.1 GHz PC with 256 GB RAM and 10 cores  
Parallel Processing

~40 hours for 1,000 sample trajectories for optimization



# DLC - Results

Flight Condition:

| Mach | $\alpha$ (deg) | $q$ (deg/sec) | Altitude (km) |
|------|----------------|---------------|---------------|
| 1.7  | 0              | 0             | 14            |

Augmented polynomial short period model:

$$\dot{e}_I = \alpha - \alpha_{cmd}$$

$$\dot{\alpha} = f(\alpha, q, \delta_e, \rho_\alpha, \rho_q, \rho_u, \lambda_u)$$

$$\dot{q} = f(\alpha, q, \delta_e, \rho_\alpha, \rho_q, \rho_u, \lambda_u)$$

Initial Conditions:

|                  | MIN  | MAX |
|------------------|------|-----|
| $\alpha_0$ (deg) | -30  | 30  |
| $q_0$ (deg/sec)  | -100 | 100 |
| $R_\alpha$       | -0.5 | 0.1 |
| $R_q$            | -7   | 5   |
| $R_u$            | -5   | 5   |
| $\Lambda_u$      | 0.25 | 3.0 |

# DLC - Results

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## Performance Metrics:

$$ATE = \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^{t_f} |e_t|$$

$$ACR = \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^{t_f} |\dot{u}_t|$$

$$CTE = \sum_{j=1}^M ATE$$

$$CCR = \sum_{j=1}^M ACR$$

$N$  number of trajectories for each analysis model

$t_f$  is the duration of each sampled trajectory

CTE is the cumulative tracking error

CCR is the cumulative control rate

TABLE II

CUMULATIVE ERROR (CTE), CONTROL RATE (CCR), AND FINAL COST

|                 | CTE     | CCR     | Cost   |
|-----------------|---------|---------|--------|
| 3-Layer RNN/GRU | 339.15  | 100.16  | 1.0438 |
| 2-Layer RNN     | 359.28  | 313.64  | 2.4970 |
| GS              | 1000.21 | 1180.04 | -      |

DLC Performance: 66% reduction in CTE, 91.5% reduction in CCR

# DLC - Results

Flight Condition:

| Mach | $\alpha$ (deg) | $q$ (deg/sec) | Altitude (km) |
|------|----------------|---------------|---------------|
| 1.7  | 0              | 0             | 14            |

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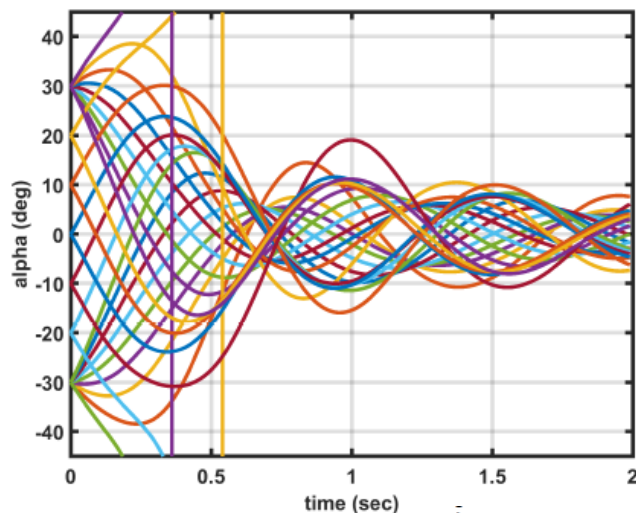
Augmented polynomial short period model:

$$\dot{e}_I = \alpha - \alpha_{cmd}$$

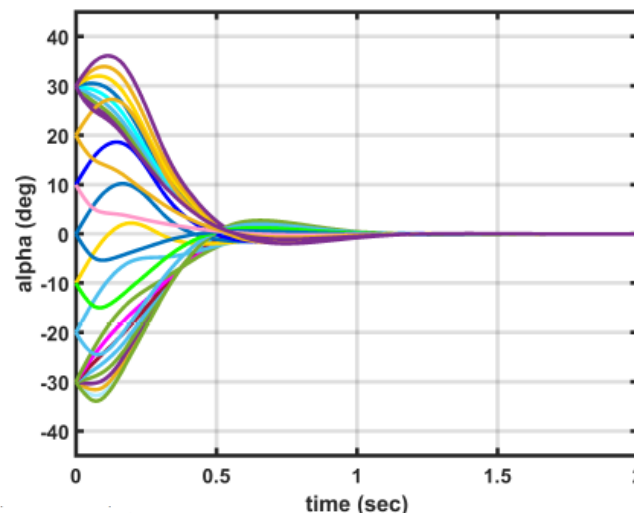
$$\dot{\alpha} = f(\alpha, q, \delta_e, \rho_\alpha, \rho_q, \rho_u, \lambda_u)$$

$$\dot{q} = f(\alpha, q, \delta_e, \rho_\alpha, \rho_q, \rho_u, \lambda_u)$$

Gain Scheduled Controller



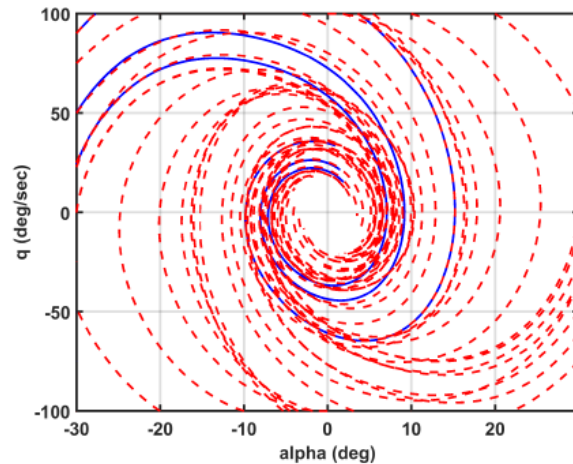
Deep Learning Controller



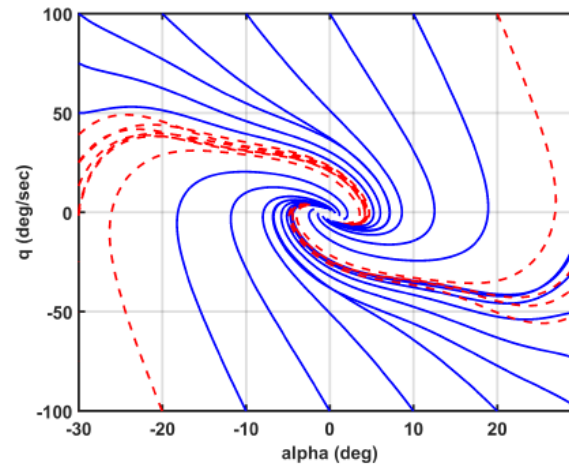
$\bar{\lambda}_u = 0.5$ ,  $\rho_u = 0$ ,  $\rho_\alpha = 0.05$ , and  $\rho_q = 2.5$

# DLC - Results

## Gain Scheduled Controller

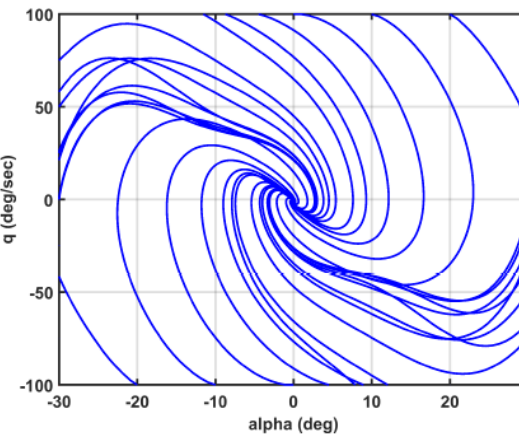


$\lambda_u = 0.75$ ,  $\rho_u = 0$ ,  $\rho_\alpha = 0.025$ , and  $\rho_q = 5$



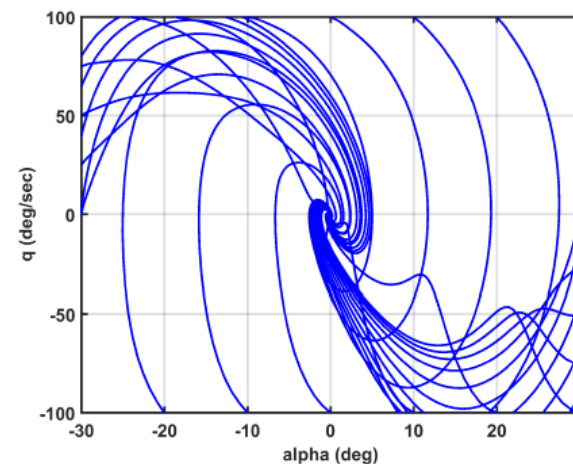
$\bar{\lambda}_u = 0.5$ ,  $\rho_u = 0$ ,  $\rho_\alpha = 0.05$ , and  $\rho_q = 2.5$

## Gain Scheduled Controller

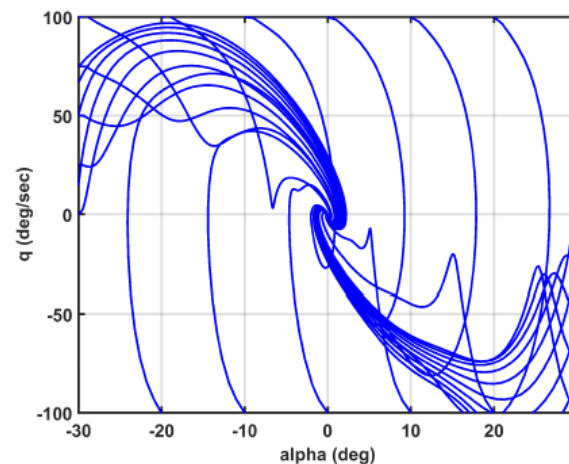


*No uncertainty or disturbances*

## Deep Learning Controller



$\lambda_u = 0.75$ ,  $\rho_u = 0$ ,  $\rho_\alpha = 0.025$ , and  $\rho_q = 5$



$\bar{\lambda}_u = 0.5$ ,  $\rho_u = 0$ ,  $\rho_\alpha = 0.05$ , and  $\rho_q = 2.5$

# Contribution and Conclusion

- Created a novel training procedure focused on bringing deep learning benefits to flight control.
- Trained controller using a set of sample trajectories that contain disturbances, aerodynamic uncertainties, and significant control attenuation/amplification in the plant dynamics during optimization.
- We found benefits of using a piecewise cost function that allows the designer to solve both robustness and performance criteria simultaneously.
- We utilized an incremental initialization training procedure for deep recurrent neural networks.



# Future Work

- Pursue a vehicle model with flexible body effects, time delays, controller effectiveness, center of gravity changes, and aerodynamic parameter variations.
- Explore improving parameter convergence and analytic guarantees: Kullback-Leibler (KL) divergence, importance sampling, etc.
- Pursue development/use of robustness analysis tools for deep learning controllers to provide region of attraction estimates and time delay margins: sum-of-squares programming etc.



# Questions?

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